

6 a  $H_0: \rho_{YX_3 | X_1} = 0$        $H_A: \rho_{YX_3 | X_1} \neq 0$

$$F(X_3 | X_1) = \frac{7010.03}{\frac{2259.16}{22}} = 68.265 \quad (1, 22 \text{ df})$$

$P < 0.001$

At  $\alpha = 0.05$  we reject  $H_0$  and conclude that  $X_3$  added to a model already containing  $X_1$  does explain a significant amount of variation in  $Y$ .

b  $H_0: \rho_{YX_2 | X_1, X_3} = 0$        $H_A: \rho_{YX_2 | X_1, X_3} \neq 0$

$$F(X_2 | X_1, X_3) = \frac{10.93}{\frac{2248.23}{21}} = 0.102 \quad (1, 21 \text{ df})$$

$P > 0.25$

At  $\alpha = 0.05$  we do not reject  $H_0$  and conclude that  $X_2$  added to a model already containing  $X_1$  and  $X_3$  does not explain a significant amount of variation in  $Y$ .

c  $H_0: \rho_{Y(X_2, X_3) | X_1} = 0$        $H_A: \rho_{Y(X_2, X_3) | X_1} \neq 0$

$$F(X_2, X_3 | X_1) = \frac{(7010.03 + 10.93) / 2}{\frac{2248.23}{21}} = 32.79 \quad (2, 21 \text{ df})$$

$P < 0.001$

At  $\alpha = 0.05$  we reject  $H_0$  and conclude that  $X_2$  and  $X_3$  added to a model already containing  $X_1$  explain a significant amount of variation in  $Y$ .

d We would include  $X_1$  and  $X_3$  in the model and omit  $X_2$ .