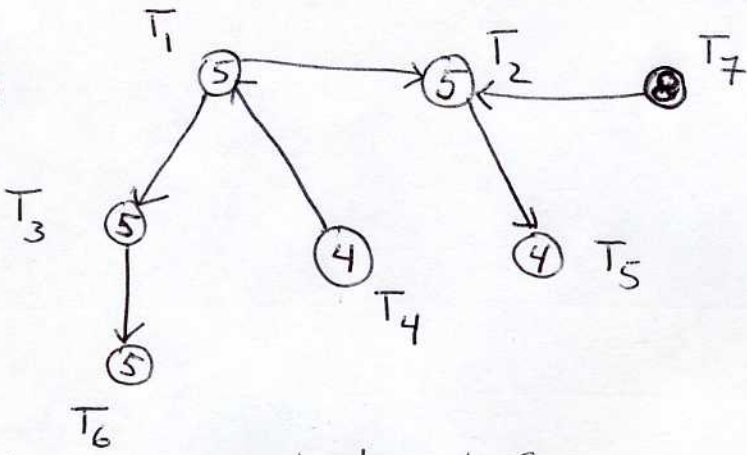


**Ex**

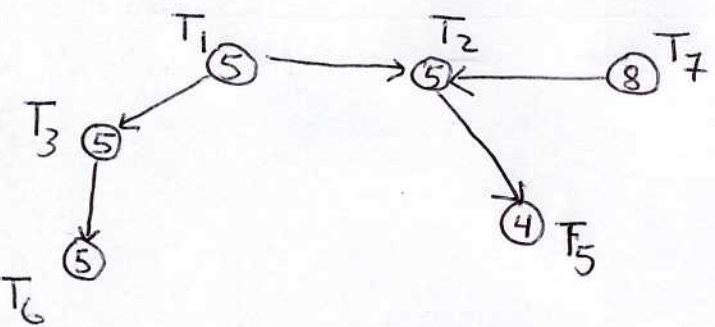


Order requirement digraph for a job. Time in minutes.

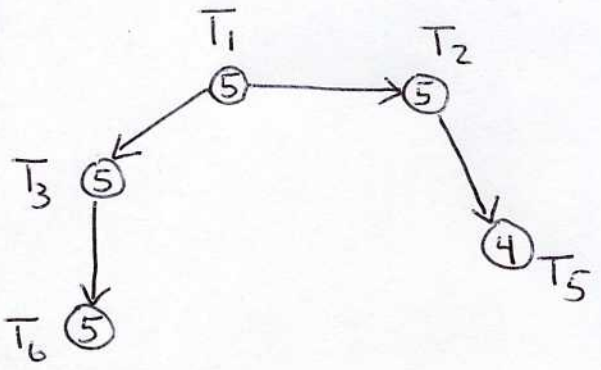
- a) what is the quickest time this job can be completed?
- b) Use critical path scheduling to create a priority list for this job.
- c) Use the priority list from b) to schedule the job on 2 processors using the list processing algorithm. How long will the job take on two processors? Could the job be sped up on 3 processors?

a) The critical path is  $T_4 T_1 T_3 T_6$ , with length 19. The quickest time this job could be completed is 19 minutes.

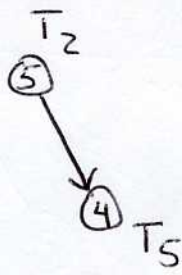
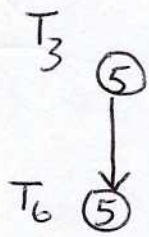
b) The task that starts the critical path goes in priority list. Priority list is  $T_4$ . Remove vertex  $T_4$  to create a new digraph.



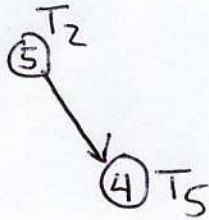
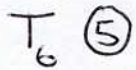
$T_7 T_2 T_5$  is critical path, length 17. Priority list is  $T_4 T_7$ .



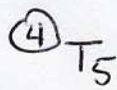
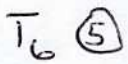
$T_1 T_3 T_6$  is critical path, length 15. Priority list is  $T_4 T_7 T_1$



$T_3T_6$  is critical path, length 10.  
Priority list is  $T_4T_7T_1T_3$

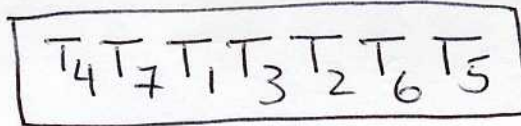


$T_2T_5$  is critical path, length 9.  
Priority list is  $T_4T_7T_1T_3T_2$



$T_6$  is critical path, length 5.  
Priority list is  $T_4T_7T_1T_3T_2T_6$

Add final vertex,  $T_5$ , to end of priority list:



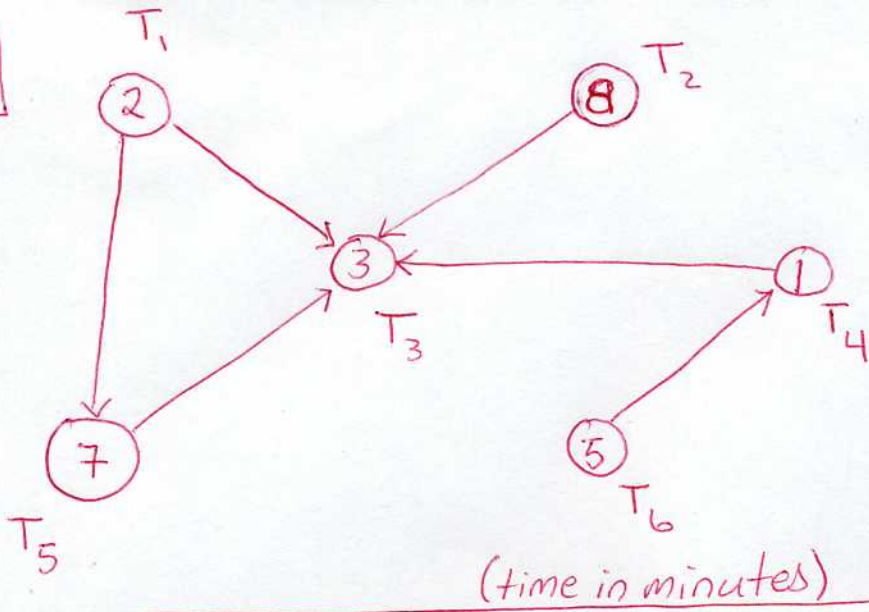
c)  ~~$T_4T_7T_1T_3T_2T_6T_5$~~

	0	4	9	14	19
Processor 1	$T_4$	$T_1$	$T_3$	$T_6$	
Processor 2	$T_7$	idle	$T_2$	$T_5$	idle
	0	8	9	14	18

The job will take 19 minutes. Since this is the length of the critical path, adding more processors will not speed up the job.



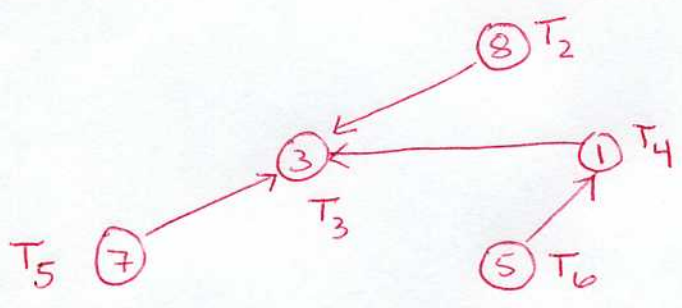
Ex



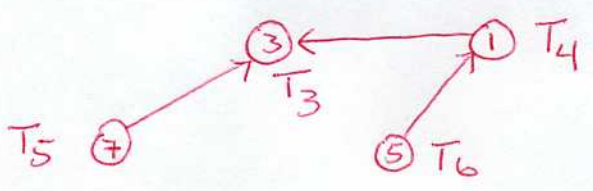
a) What is the quickest time the job represented by the order requirement digraph could be completed?  
 The length of the critical path ( $T_1, T_5, T_3$ ) is 12, so this is the fastest the job could be completed.

b) Use critical path scheduling to create a priority list for the above order requirement digraph.

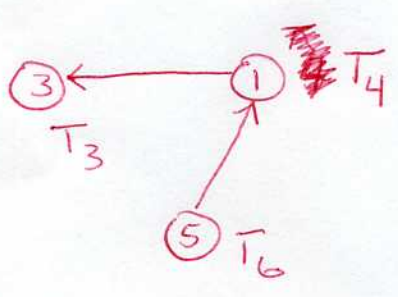
Critical path is  $T_1, T_5, T_3$ , length 12. Put  $T_1$  in the priority list, and remove  $T_1$  from digraph:



$T_2, T_3$  is critical path, length 11.  
 Priority list is  $T_1, T_2$



$T_5, T_3$  is critical path, length 10.  
 Priority list is  $T_1, T_2, T_5$



Only one path left. So add  $T_6, T_4$ , then  $T_3$  to priority list.

Priority list from critical path schedule is  $T_1, T_2, T_5, T_6, T_4, T_3$ .

c) use the priority list from part b) to schedule the job on 2 processors. How long will the job take? Could the job be speeded up on 3 processors?

~~T<sub>1</sub>~~ ~~T<sub>2</sub>~~ ~~T<sub>5</sub>~~ ~~T<sub>6</sub>~~ T<sub>4</sub> T<sub>3</sub>

	0	2	9	13	14	17
Processor 1	T <sub>1</sub>	T <sub>5</sub>	idle	T <sub>4</sub>	T <sub>3</sub>	
Processor 2	T <sub>2</sub>		T <sub>6</sub>			
	0		8	13		

The job would take 17 minutes. Since this is longer than the length of the critical path, it would be speeded up on 3 processors.

d) schedule the job on 3 processors.

~~T<sub>1</sub>~~ ~~T<sub>2</sub>~~ ~~T<sub>5</sub>~~ ~~T<sub>6</sub>~~ ~~T<sub>4</sub>~~ T<sub>3</sub>

	0	2	9	12
Processor 1	T <sub>1</sub>	T <sub>5</sub>		T <sub>3</sub>
Processor 2	T <sub>2</sub>		idle	
Processor 3	T <sub>6</sub>	<del>T<sub>4</sub></del>	idle	
	0	5	6	8

The job would take 12 minutes.