## Instructions

- Complete solutions will include well labeled graphs, good explanation of the process used to implement any algorithms, and complete sentences for any discussion of the answer. Where appropriate, you can draw circuits or number edges directly on the graphs provided.
- You may talk about the assignment with other students in the class, but the work you submit must be your own independent creation. If you have questions talk with me before or after class or during office hours.


## Questions

1. (20 marks) The following represents a house with a variety of rooms and doors, some of which lead outside.
(a) Can you start in one of the rooms, and walk through every door only once? Explain your answer by constructing a graph of the situation, clearly explaining what the edges and vertices are in terms of the house.
(b) Can you start in one of the rooms, and walk through every door only once and end back where you started?
(c) If the answer to (b) is no, what is the least number of doors you would need to add to make the answer to (b) be yes? In which rooms would these extra doors be placed?

2. (20 marks) You may answer this question directly on this sheet.
(a) For the following graphs, identify an Euler circuit for the graph by numbering the edges in the order they are traversed.

(b) Determine a most efficient Eulerization of the following graphs.

(i)

(ii)

(iii)

3. (20 marks) Kohl's Department Store has eleven distributions centers.
(source: http://www.kohlscareers.com/distribution/about/ accessed 1/8/13)
The distances (in miles) between the distribution centers is given in the following table.
(source: http://www.mapquest.com/ accessed $1 / 20 / 10$ )

|  |  |  | $\begin{aligned} & \text { 岂 } \\ & \text { Z } \\ & \text { III } \end{aligned}$ |  |  |  |  | $\begin{aligned} & \pi \\ & \stackrel{\pi}{3} \\ & \stackrel{0}{0} \end{aligned}$ |  | $\begin{aligned} & \ddot{U} \\ & 0 \\ & \ddot{0} \\ & \ddot{Z} \\ & 0 \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Grain Valley, MO | - | 567 | 668 | 863 | 1188 | 579 | 569 | 422 | 1557 | 996 | 1839 |
| Corsicana, TX | 567 | - | 1156 | 850 | 1633 | 1076 | 1150 | 920 | 1438 | 1320 | 1706 |
| Findlay, OH | 668 | 1156 | - | 703 | 561 | 384 | 56 | 332 | 2239 | 424 | 2400 |
| Macon, GA | 863 | 850 | 703 | - | 964 | 908 | 701 | 825 | 2215 | 651 | 2480 |
| Mamakating, NY | 1188 | 1633 | 561 | 964 | - | 890 | 506 | 838 | 2742 | 314 | 2907 |
| Menomonee Falls, WI | 579 | 1076 | 384 | 908 | 890 | - | 409 | 175 | 2010 | 751 | 2174 |
| Middletown, OH | 569 | 1150 | 56 | 701 | 506 | 409 | - | 355 | 2266 | 369 | 2423 |
| Ottawa, IL | 422 | 920 | 332 | 825 | 838 | 175 | 355 | - | 1906 | 700 | 2073 |
| San Bernardino, CA | 1557 | 1438 | 2239 | 2215 | 2742 | 2010 | 2266 | 1906 | - | 2568 | 355 |
| Winchester, VA | 996 | 1320 | 424 | 651 | 314 | 751 | 369 | 700 | 2568 | - | 2767 |
| Patterson, CA | 1839 | 1706 | 2400 | 2480 | 2907 | 2174 | 2423 | 2073 | 355 | 2767 | - |

a) How many distinct Hamiltonian circuits are there between the distribution centers? Say you have access to a computer that can calculate one thousand Hamiltonian circuits in a second. How long would it take for your computer to implement a brute force method of determining the optimal Hamiltonian circuit? Is this problem one suitable for solution (by a computer!) using the brute-force algorithm?
b) You are the Executive Secretary to the boss, and need to plan a road trip tour of the eleven distribution centers. Using the nearest neighbor algorithm starting and ending at Ottawa, decide what the tour should look like and the length of the tour.
c) Your boss decides to pay for a flight back from the last city visited to Ottawa, so you only need to find a Hamiltonian path beginning at Ottawa and visiting all the cities. Both nearest neighbour and sorted edges can be modified to find Hamiltonian paths by simply not including the last edge that creates the Hamiltonian circuit. Would it be be better, in general, to use a nearest neighbour algorithm starting at Ottawa or sorted edges algorithm to determine the Hamiltonian path? Justify your choice by referring to the properties of the two algorithms.

