The test will have five types of problems:

- (10 Questions × 1 mark each = 10 marks total) Matching
- $(10 \times 1 \text{ mark} = 10 \text{ marks})$ True or False
- $(10 \times 2 \text{ marks} = 20 \text{ marks})$ Multiple Choice
- $(6 \times 5 \text{ marks} = 30 \text{ marks})$ Short Answer
- $(3 \times 10 \text{ marks} = 30 \text{ marks}) \text{ Long Answer}$

Section 1. (10 \times 1 mark = 10 marks) Matching Match term or quantity in left column to descriptions that best apply from the numbered columns.

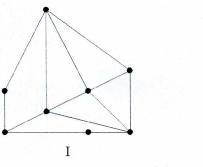
- 1. a circuit on the graph that visits each vertex once and only once.
- 2. the shortest path in an order requirement digraph.
- 3. for every pair of its vertices there is at least one path connecting the two vertices.
- 4. the longest path in an order requirement digraph.
- 5. finding a circuit on a graph that covers every edge of the graph at least once and reuses the least number of edges (or if the edges have wights, has the circuit has the shortest length).
- 6. a heuristic algorithm for solving the traveling salesman problem (TSP) by determining a Hamiltonian circuit.
- 7. an algorithm that solves the minimum cost spanning tree problem.
- 8. a heuristic algorithm for assigning tasks to processors.
- 9. a heuristic algorithm for determining a good priority list from an order requirement digraph (ORD).
- 10. a circuit that covers each edge of a graph once, but not more than once.
- 11. an assignment of colors to the edges of a graph such that no two vertices joined by an edge have the same color.
- 12. a graph where every vertex is joined by an edge to every other vertex.
- 13. a subgraph of a connected graph that is a tree and includes all the vertices of the original graph.
- 14. the set of points which are possible solutions to a linear programming problem.
- 15. an assignment of colors to the vertices of a graph such that no two vertices joined by an edge have the same color.

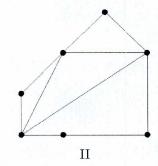
feasible region 14

Section 2. True or False Circle True (T) or False (F):

Section 3. Multiple Choice Circle the most appropriate answer:

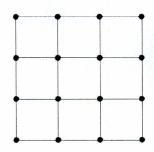
(1) Which of the following graphs have Euler circuits?





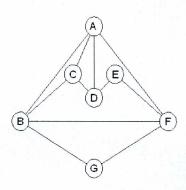
- A) I only
- (B) It only
- C) I and II both
- D) Neither I nor II

(2) In order to culcrize the graph below, what is the fewest number of edges that need to be duplicated?

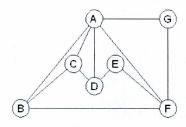


- A) 2
- B) 3
- (C) 4)
- D) 6
- (3) For which of the two situations below is it desirable to find an Euler circuit or an efficient eulerization of a graph?
 - I. A city employee must check the traffic signals at each intersection in downtown area to be certain they are working.
 - II. An employee of a power company reads the electric meters outside each house along the streets in a residential area.
 - A) I only
- B) I only
- C) I and II both
- D) Neither I nor II
- (4) For the travelling salesman problem (Hamiltonian circuit) applied to four cities, how many <u>distinct</u> Hamiltonian tours are possible?
 - (A) 3
- B) 6
- C) 12
- D) 24

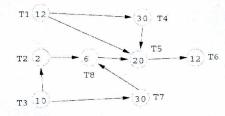
(5) Which of the following describes a Hamiltonian circuit for the following graph?



- A) AFEDCBG
- B) ADEFGBA
- C) ABCDEFGBA
- (D) BGFEDCA
- (6) A talent show producer needs to fit 17 acts of varying length into several segments. The segments will be no more than 45 minutes long, and are to be separated by intermissions. This problem could be solved by using
 - A) a Hamiltonian circuit.
 - B) linear programming.
 - C) the critical path scheduling algorithm.
 - D) none of these techniques would work to find a solution.
- (7) Which of the following represents a spanning tree for the following graph?



- A) AG,GF,FB,AB B) AD,EF,DE,AG,DC,AB C) AD,EF,DE,AG,BC,AB D) Both B) & C)
- (8) What is a critical path for the following order requirement digraph (with time given in minutes)?



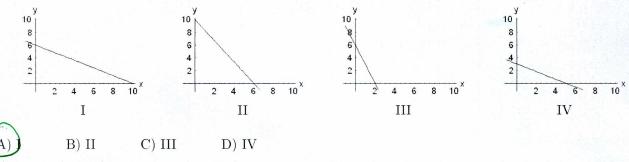
A) T1,T4,T5,T6 B) T3,T2,T8,T5,T6 C) T3,T7,T8,T5,T6 D) Both B) & C)

(9) A company has a job scheduled on two processors in the following manner. To shorten the time needed to complete the job, the company plans to shorten the time spent on task T3. By how much can the time to complete T3 be reduced before there is no benefit in reducing it further?

1	T1=12	T4=8	T3=7	T2=6	T5=2
2			T7=11		T6=3

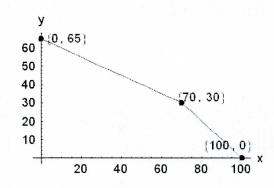
A) 0 (B) 2 C) 4 D) 7

- (10) A spanning tree on a graph H:
 - A) includes all the vertices on the graph H.
 - B) may contain a circuit.
 - C) is connected.
 - (D) Both A) & C).
- (11) The graph of the equation 3x + 5y = 30 is



- (12) The point of intersection of the lines whose equations are 2x + 3y = 12 and x + 5y = 13 is
 - $\frac{A)}{B}$ (2, 3)
 - B) (3, 2)
 - (6,0)
 - D) (-2,3)
- (13) Write the constraint equations for the following situation: A cheeseburger requires 5 oz of meat and 0.7 ounces of cheese while a superburger requires 7oz of meat and 0.6 oz of cheese. The burger stand has 350 oz of meat and 42 oz of cheese available. The profit on a cheeseburger is 10 cents and the profit on a superburger is 40 cents.
 - (A) 5) $+7y \le 350$, $0.7x + 0.6y \le 42$, $x \ge 0$, $y \ge 0$. B) $5x + 0.7y \le 350$, $7x + 0.6y \le 42$, $x \ge 0$, $y \ge 0$.
 - C) $5x + 7y \le 10$, $0.7x + 0.6y \le 42$, $x \ge 0$, $y \ge 0$.
 - D) $10x + 4y \le 350$, $0.7x + 0.6y \le 42$, $x \ge 0$, $y \ge 0$.
- (14) Suppose in a linear programming problem you find the feasible region has corner points of (0,0), (5,0), (0,4) and (2,3). If the profit formula is P = \$3x + \$4y, then the maximum profit is
 - A) \$12
 - B) \$13
 - C) \$14
 - D) \$18

Problems (15)-(17) are related the following sketch of a feasible region:

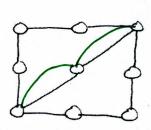


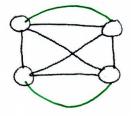
- (15) What is the maximum profit when P = \$3x + \$4y?
 - A) \$260 ...
- C) \$300
- D) \$370
- (16) What values of x and y produce the maximum profit when P = \$4x + \$4y?
 - A) only x = 0, y = 65y = 0 and x = 70, y = 30
- B) only x = 70, y = 30E) none of the above
- C) only x = 100, y = 0 D) only x = 100.

- (17) Which point is not in the feasible region?
 - A) (0,0)
- B) (60, 30)
- C) (30,60)
- D) (70, 30)

Section 4. Short Answer

(1) Find the most efficient Eulerization of the following graphs:







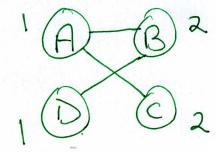
(a)

(b)

(c)

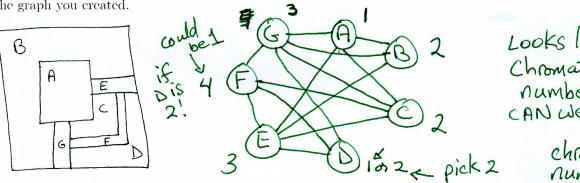
		Α	В	\mathbf{C}	D	
	A		X	X	- 214	-
(2) The following table represents scheduling conflicts between individuals.	В	X			X	
	С	\mathbf{X}				
	D		X			

Construct a graph that conveys this information. What is the chromatic number of the graph you created?



chromatic number is 2.

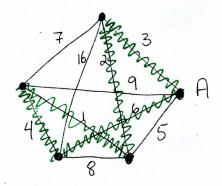
(3) Create a graph that can used to help you color the following map. Then, determine the chromatic number of the graph you created.



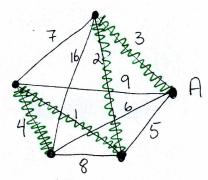
Looks like. Chromatic number is 4. CAN We do better?

> chromatic number is 3

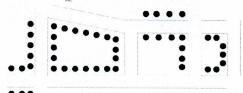
(4) For the following graph, use the <u>nearest neighbour algorithm</u> starting at vertex A to determine a Hamiltonian circuit. You can simply highlight the included edges on the graph.



(5) For the following graph, use <u>Kruskal's algorithm</u> to determine a minimum cost spanning tree. You can simply highlight the included edges on the graph.



(6) For following street network, the dots represent parking meters which much be checked by a patrol officer on foot. Draw a graph beside the network which would be useful to help them find an efficient route.

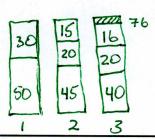




(7) Use the decreasing version of the First Fit Algorithm to schedule advertisements of lengths 30.40.15.20.19.45.50.20 seconds in second slots for a radio program.

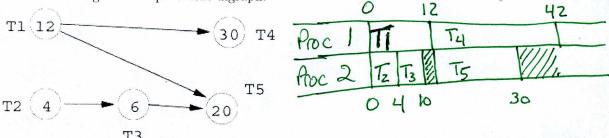
First Fit Algorithm Put items into the first bin until the next item doesn't fit. Then open a new bin, but leave the first bin open. Put each item from the list into the lowest numbered bin in which it will fit, opening new bins when an item won't fit in any of the open bins.

Decreasing -> resider list 50,48,40,30,20,20,16,15



Section 5. Long Answer

(1) Use critical path scheduling and then the list processing algorithm to construct a schedule on two processors for the following order requirement digraph.



Priority List T, T2 T4 T3 T5

(2) Sketch the feasible region for the following linear programming mixture problem, and then determine how many of each type of house should be produced to maximize profit. A mixture chart is not required for your solution, although it may help you solve the problem.

Kim and Lynn produce pottery vases and bowls. A vase requires 25 of clay and 5 oz of glaze. A bowl requires 20 oz of clay and 10 oz of glaze. There are 500 oz of clay and 160 oz of glaze available. The profit on one vase is \$5 and the profit on one bowl is \$3.

	Clay(02)	Glaze (02)	Minimum	Profit
Vases X	25	5	0	#5
Bowlsy	20	10	0	#3
0	500	160		

Constraints: 25x+2045500 25x+204=500 Test point (0,0):

25(0) +20(0) =500 0 500 True

shade below line.

5x+10y=160 5x+104=160 Test Point (0,0): 5(0)+10(0) = 160

0 = 160 True

shade side with (0,0)

Clay: 25x+20y 5500 Glaze: 5x+10y 5160

intersection (12,10).

Profit P=5x+34

X=0

intersection solve 5x+10y=160 for x = 160-104 = 160 - 104 = 32-24 Sub into 25x + 204 = 500

Intersection is (12,10) Get X=32-2(10)=12.

Corner Point | Profit = 5x+34 x=0 y=0 x=0 y=16

#48
#100 = Max profit is #100 when
#100 = they make 20 vases
#90 and no bowls.

(3) When two towns are within 145 miles of each other, the frequency used by a certain type of emergency response system for the towns requires that they be on different frequencies to avoid interference with each other.

The following table shows mileage distance between six towns.

	A	В	С	D	E	F
A		290	277	168	303	133
В	290		(132)	(83)	79	201
С	277	(132)		153	(58)	164
D	168	(83)	153		(140)	71
Е	303	79	(58)	(140)	- 35	196
F	133	201	164	(71)	196	

Vertex Colowing!

Put an X whenever

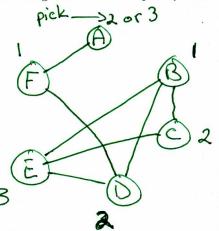
distance is less than

145 miles or I just

chose to circle them

- 1. What are minimum number of frequencies that are needed for each town to have its emergency broadcasts not interfere with neighbouring towns?
- 2. How many different towns would be assigned to each frequency used?

Graph: Vertices: towns dedges: between towns closer than 145 miles.



Fequency	town
1	BF
Z	CDA:
3	E
	1

(4) For the following order requirement digraph and priority list $T_1, T_5, T_6, T_2, T_4, T_3, T_8, T_9, T_7, T_{10}$, determine a schedule on three processors using the list processing algorithm.

