

There will be no Descartes's Rule of Signs on the Test.

### Discussion

Make some notes on the questions, then discuss what you wrote with a partner. Make note of anything that you and your partner disagree on, or that you had difficulty with.

1. Write down in words the things you need to sketch a polynomial.
2. Write down in words the things you need to sketch a rational function.
3. What are the three types of asymptotes? Draw example sketches of each, and include correct limit notation to explain each asymptote.
4. What do you use a sign chart to do? Why?
5. Explain in words how you solve the following types of equations:
  - Equations involving square roots
  - Equations of quadratic type
  - Equations involving absolute values
6. Explain the technique in words to factor  $f(x) = 12x^3 - 16x^2 + 7x - 1$ .
7. Explain what an extraneous solution is.
8. Explain what a hole is, in relation to a rational function.
9. How can you tell if a function changes sign at a zero or vertical asymptote?

### Computation

Work out solutions, and discuss with a partner as needed. Make sure your solutions are well organized, complete, and use correct mathematical notation. Make sure any sketch you draw is labelled.

10. Solve  $\sqrt{x^2 + 1} + \sqrt{x^2 - 2} = 7$ .
11. Sketch  $f(x) = \frac{(3x - 1)^2(x + 1)}{(x - 1)^3}$ .
12. Solve  $|2x - x^2| = 2x - 4$ .
13. Solve  $|2x| = 2 - |x|$ .
14. Find all real and complex valued solutions to  $12x^4 - 16x^3 + 36x^2 - 48x = 0$ .
15. Determine, in interval notation, the solution to  $x \leq \frac{1}{(x - 2)^2}$ .
16. Sketch  $g(x) = \frac{(3x - 1)^2x}{(x - 1)^2}$ .
17. Sketch  $f(x) = 7(2 - x)^3(x^2 - 2x + 1)$ .
18. Solve  $(x^2 + 2x)^2 - (x^2 + 2x) - 2 = 0$ .