You should be able to answer questions dealing with these concepts. Study the practice problems, guided examples, WeBWorK, and examples worked in the textbook, as well as the practice test.

## Previous work that will be needed

- composition of functions
- quadratic formula
- inverse functions
- transforming functions
- basic properties of functions (domain, range, symmetry, etc)
- average rate of change (could be one involving square root, fractions, or powers)

## Exponential, Logistic, and Logarithmic Functions

- exponential functions  $y = e^{kx}_c$  or  $y = b^x$
- logistic functions  $y = \frac{c}{1 + ae^{-kx}}$ 
  - properties of exponents: If x and y are real numbers, and b > 0 is real, then

1. 
$$b^x \cdot b^y = b^{x+y}$$

2. 
$$\frac{b^x}{dt} = b^{x-y}$$

$$b^y$$

- 3.  $(b^x)^y = b^{xy}$
- nomenclature: base, exponent
- exponential growth (b > 1) and exponential decay (0 < b < 1)
- the natural base e
- the basic functions  $y = e^x$  and  $y = \ln x$
- sketching and transforming exponential functions
- constructing exponential population models
- logarithmic functions  $f(x) = \log_b x$ 
  - interpreted as the inverse function of the exponential function
  - sketching and transforming logarithmic functions
  - properties of logarithms: If x and y are positive numbers, and  $b > 0, b \neq 1$  is real, then
    - 1.  $\log_b(xy) = \log_b x + \log_b y$

2. 
$$\log_b\left(\frac{x}{y}\right) = \log_b x - \log_b y$$

- 3.  $\log_b(x^r) = r \log_b x$  where r is any real number
- change of base
- common logarithms  $(y = \log x)$  and natural logarithms  $(y = \ln x)$
- solving equations involving logarithms and exponentials
  - extraneous solutions