

## Study Guide

Here is a study guide for the course. We may, as the course progresses, be emphasizing slightly different aspects. But for now, this is the trip we are embarking upon, with the local points of interest mapped out before us, serving to whet our appetite for discovery.

How should you use a study guide? Well, you should **not** ignore it until the night before an exam! You should be referring to it continually, *expanding* or *deleting* it as you see fit with details and worked examples. With this extra layer of detail you will then have excellent study notes for exams, and later reference.

[Review Notes for Chapter 1](#) are available online. I will only give you these for Chapter 1 since a major benefit of review notes is gained from creating them yourself!

### *Mathematica*

the library of *Mathematica* commands we understand will grow throughout the year  
keep a list of the basic commands we use and practice!

### Functions and Models

#### **1.1 Four Ways to Represent a Function**

the definition of a function  
the four representations  
definition of domain, range, increasing, decreasing  
piecewise defined functions  
even and odd functions

#### **1.2 Mathematical Models**

the modeling process  
interpolation and extrapolation  
classes of functions

#### **1.3 New Functions from Old Functions**

mechanics and geometry of transforming functions  
adding, subtracting, multiplying and dividing functions  
composition

#### **1.5 Exponential Functions**

properties  
translation and reflection  
exponential functions as models for growth and decay  
growth rates of exponentials as compared to polynomials

#### **1.6 Inverse Functions and Logarithms**

logarithmic functions  
one-to-one functions

### Limits and Derivatives

#### **2.1 The Tangent and Velocity Problems**

the tangent line viewed as the limit of secant lines  
average versus instantaneous  
zooming in and local linearity  
approximating the slope

#### **2.2 The Limit of a Function**

various meanings of limit  
geometric and limit definitions of vertical asymptotes  
can we numerically compute a limit?

#### **2.3 Calculating Limits Using the Limit Laws**

algebraic computation of limits

graphical evaluation

examples of when limits don't exist

computing limits when limit laws do not apply

### **2.5 Continuity**

graphical and mathematical definitions of continuity

examples of discontinuity

The Intermediate Value Theorem

### **2.6 Limits at Infinity; Horizontal Asymptotes**

geometric and limit definitions of horizontal asymptotes

computation of infinite limits

the danger of using computers to check limits

### **2.7 Tangents, Velocities, and Other Rates of Change**

slope of tangent line as limit of slope of secant lines

instantaneous rate of change as limit of average rate of change

### **2.8 Derivatives**

notation

equation of tangent line

discrete data approximation

units of the derivative

### **2.9 The Derivative as a Function**

differentiable functions

how a function fails to be differentiable

sketching derivative function from the graph of the original function

## Differentiation Rules

### **3.1 Derivatives of Polynomials and Exponential Functions**

the power rule

the definition of  $e$

### **3.2 The Product and Quotient Rules**

use of the rules

justification of the rules

### **3.3 Rates of Change in the Natural and Social Sciences**

### **3.4 Derivatives of Trigonometric Functions**

### **3.5 The Chain Rule**

use of the chain rule

justification of the chain rule

### **3.6 Implicit Differentiation**

implicit functions and implicit curves

the technique of implicit differentiation

the derivatives of inverse trigonometric functions

### **3.7 Higher Derivatives**

second and higher derivatives

physical meaning of higher derivatives

### **3.8 Derivatives of Logarithmic Functions**

logarithmic differentiation

the concept of  $e$  as a limit

### **3.10 Related Rates**

concept of related rates

procedure for handling related rates

THE VALUE OF WELL LABELED DIAGRAMMS AND GOOD NOTATION

### **3.11 Linear Approximation and Differentials**

linearization

the differential

## Application of Differentiation

**4.1 Maximum and Minimum Values**

intuitive and precise definitions of local and absolute extrema

The Extreme Value Theorem

critical values

**4.3 How Derivatives affect the Shape of a Graph**

first derivative: increasing or decreasing

tests for maxima and minima

second derivative: concavity and points of inflection

**4.4 Indeterminate Forms and L'Hospital's Rule**

types of indeterminate forms

use of L'Hospital's Rule

**4.7 Optimization Problems**

how to set up and solve optimization problems

first derivative test for absolute extrema

checking results graphically

useful techniques to solve problems

**4.9 Newton's Method**

Newton's method and its uses

Geometric interpretation

speed of approximation

**4.10 Antiderivatives**

antiderivatives with and without initial conditions

position, velocity, acceleration

direction fields

## Integrals

**5.1 Areas and Distances**

area under a curve as the limit of a sum of areas of rectangles

distance in terms of the velocity curve

Riemann sums

approximating of areas using rectangles

**5.2 The Definite Integral**

the precise definition of a definite integral

the concept of area versus signed area

the geometric and comparison properties of definite integrals

**5.3 The Fundamental Theorem of Calculus**

FTC1

FTC2

**5.4 Indefinite Integrals and Total Change Theorem**

definitions

**5.5 The Substitution Rule**

## Multivariable Calculus