

CSci 1302 Assignment 3

Due Wedn., Sept. 20 in class

Problem 1 (6 points). Exercises 10, 11, 12 p. 41.

Problem 2 (6 points). Exercises 42, 44 p. 43.

Problem 3 (20 points). Prove the following using deductive proofs (not truth tables).

1.
$$\frac{(p \vee q) \rightarrow r}{\therefore \sim r \rightarrow \sim p}$$
2.
$$\frac{\sim(p \rightarrow q) \quad p \rightarrow r}{\therefore r}$$
3.
$$\frac{p \wedge \sim r \quad (q \rightarrow r)}{\therefore \sim(p \rightarrow q)}$$
 (use proof by contradiction)
4.
$$\frac{(p \wedge q) \leftrightarrow r}{\therefore (r \rightarrow p) \wedge (r \rightarrow q)}$$
5.
$$\frac{(p \vee q) \leftrightarrow r}{\therefore (p \rightarrow r) \wedge (q \rightarrow r)}$$

Problem 4 (6 points). Which of the following two arguments are valid (if any)? Justify your answer the following way: use deductive proofs or truth tables to prove a valid argument; show at least one row of the truth table to disprove an invalid argument.

You might want to guess the answer first, and then check your intuition.

$$A. \quad \frac{(p \vee q) \rightarrow s \quad (q \vee r) \rightarrow s}{\therefore q \rightarrow s}$$

$$B. \quad \frac{(p \wedge q) \rightarrow s \quad (q \wedge r) \rightarrow s}{\therefore q \rightarrow s}$$