CSci 1302 Assignment 9 Due Wednesday, April 1 in class

Problem 1 (2 points). Exercise 27 p. 234.

Problem 2 (5 points). Fibonacci numbers are defined as $F_0 = 0, F_1 = 1$, and for all $k \ge 2$ $F_k = F_{k-1} + F_{k-2}$. Use strong induction to prove the following property of Fibonacci numbers: $F_{n+m-2} = F_n F_{m-1} + F_{n-1} F_{m-2}$. Here $n \ge 2, m \ge 2$. Please point out the part of the proof where you had to use strong induction.

Hint: you should do induction on n only and assume that m is fixed. The other way around (induction on m with n fixed) should work as well, but you cannot do induction on both.

Problem 3 (10 points). Exercises 2, 3, 6 (note that $\lfloor k/2 \rfloor$ denotes k/2 rounded down), 16 pp. 242-243.